

# **Towards verification of Bluetooth device discovery**

Marie Duflot

# Outline

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- Description of the protocol
- Modelling
- First results
- We want more ....

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# Description of the protocol

# Protocol overview

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- short-range low-power wireless protocol
- frequency hopping over 79/32 frequencies

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  - no communication before initialisation

# Protocol overview

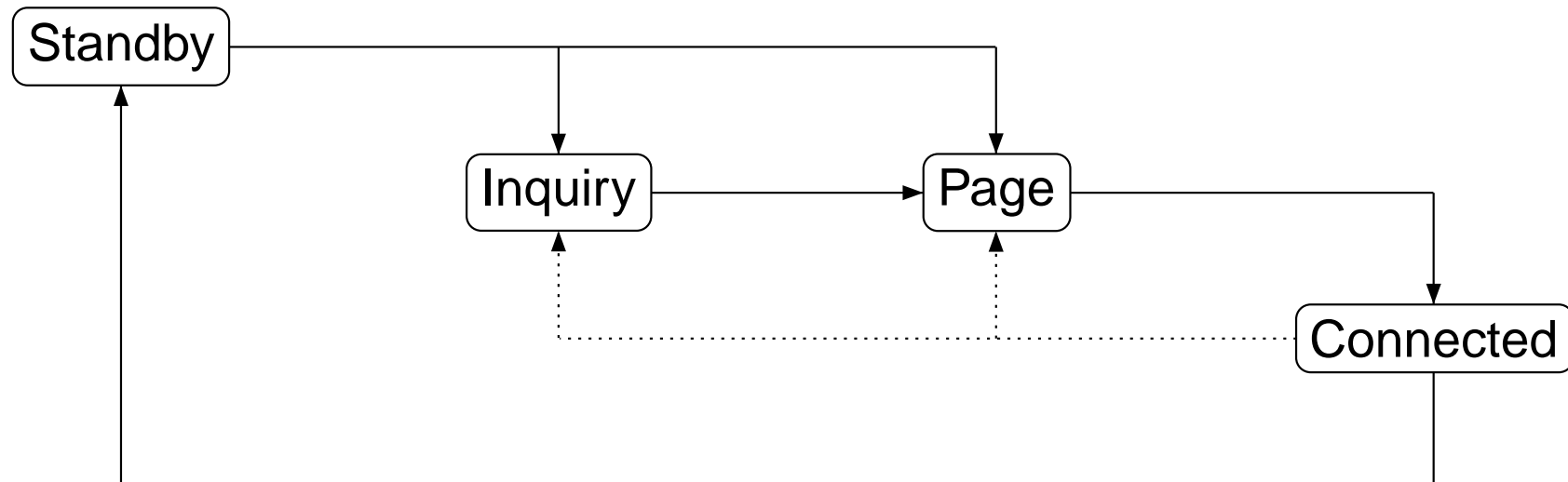
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  - need to form piconets
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First mandatory step: device discovery

# States of a Bluetooth device

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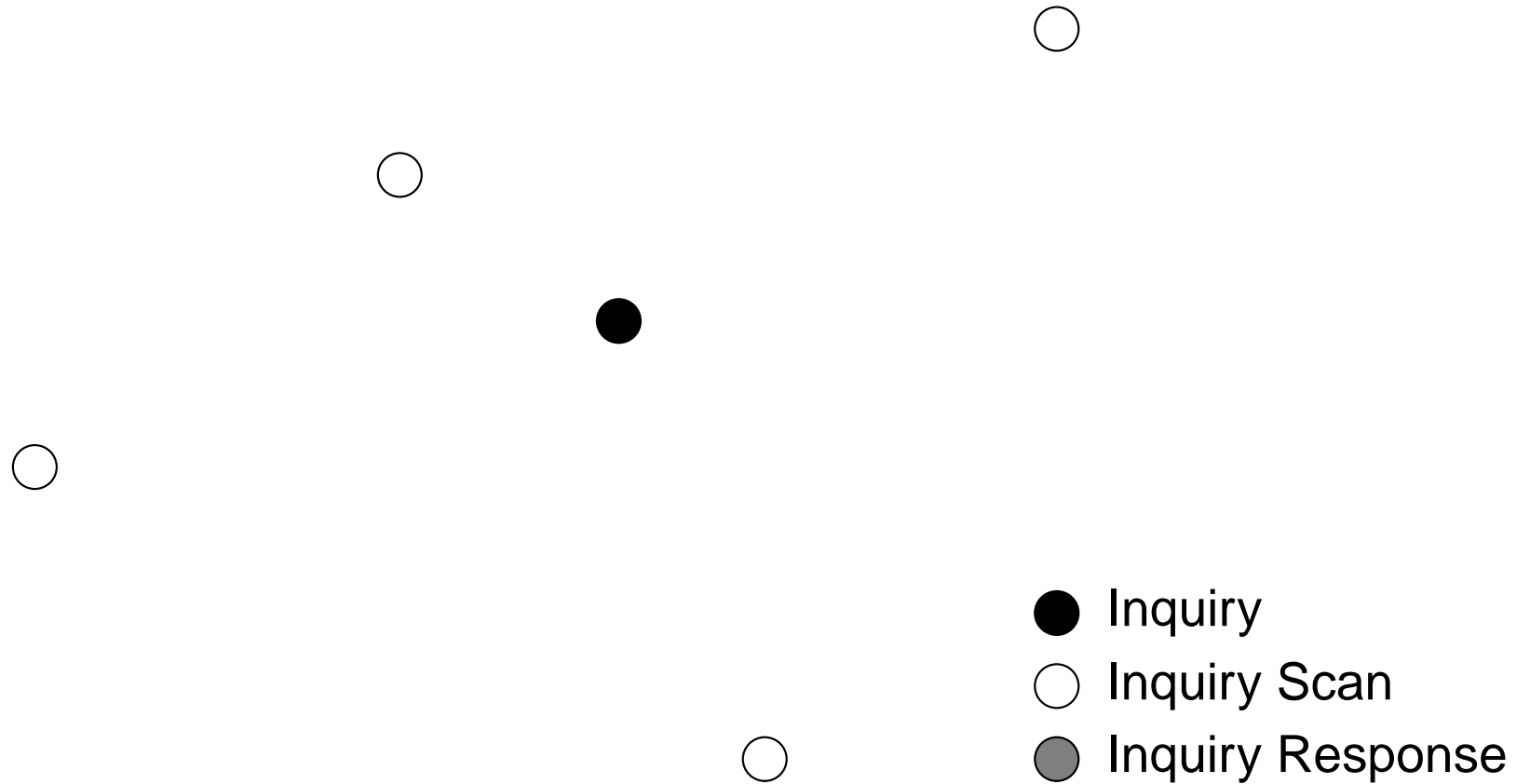
Standby: default operational state

Connected: device ready to communicate in a piconet



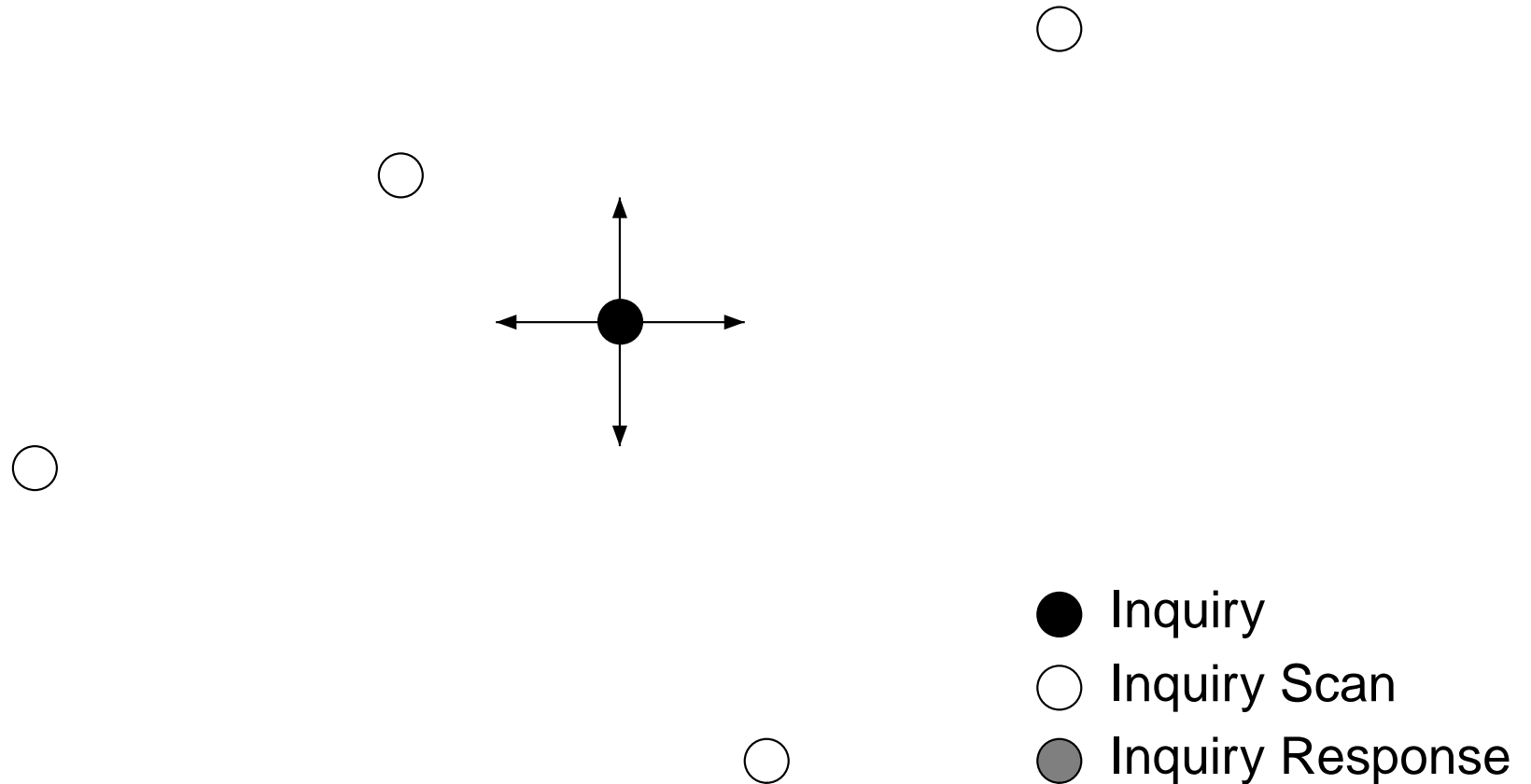
# Inquiry (version 1.2)

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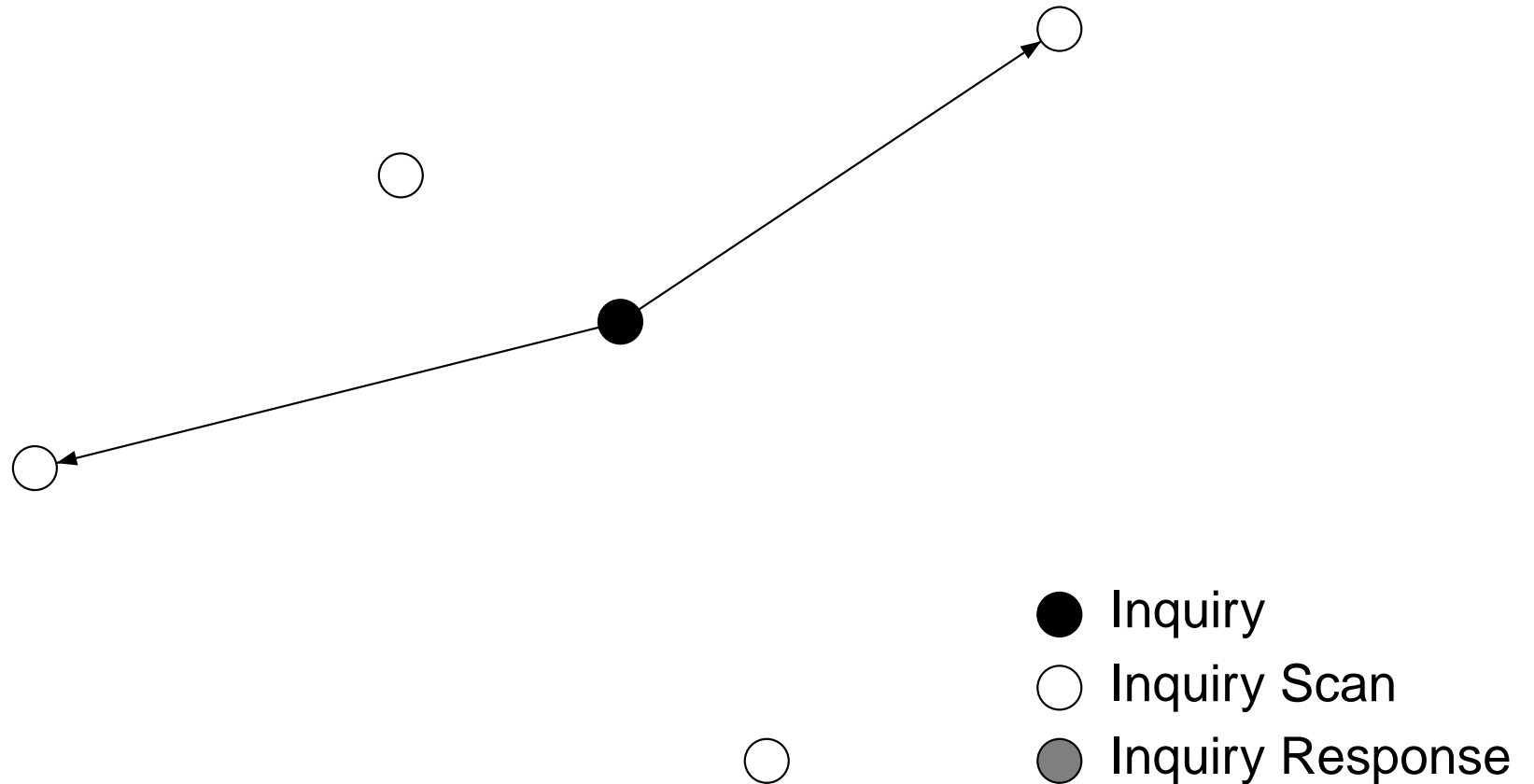
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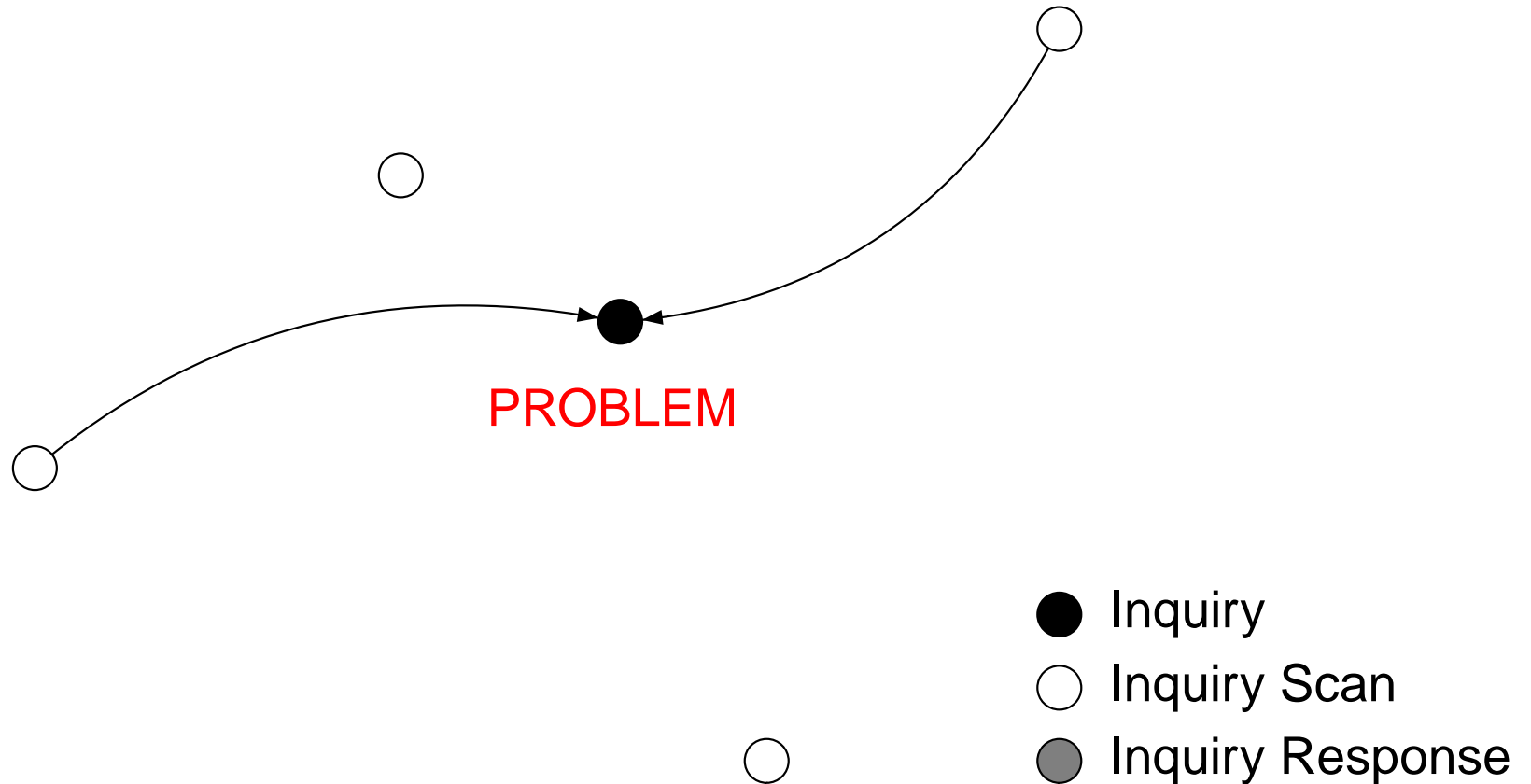
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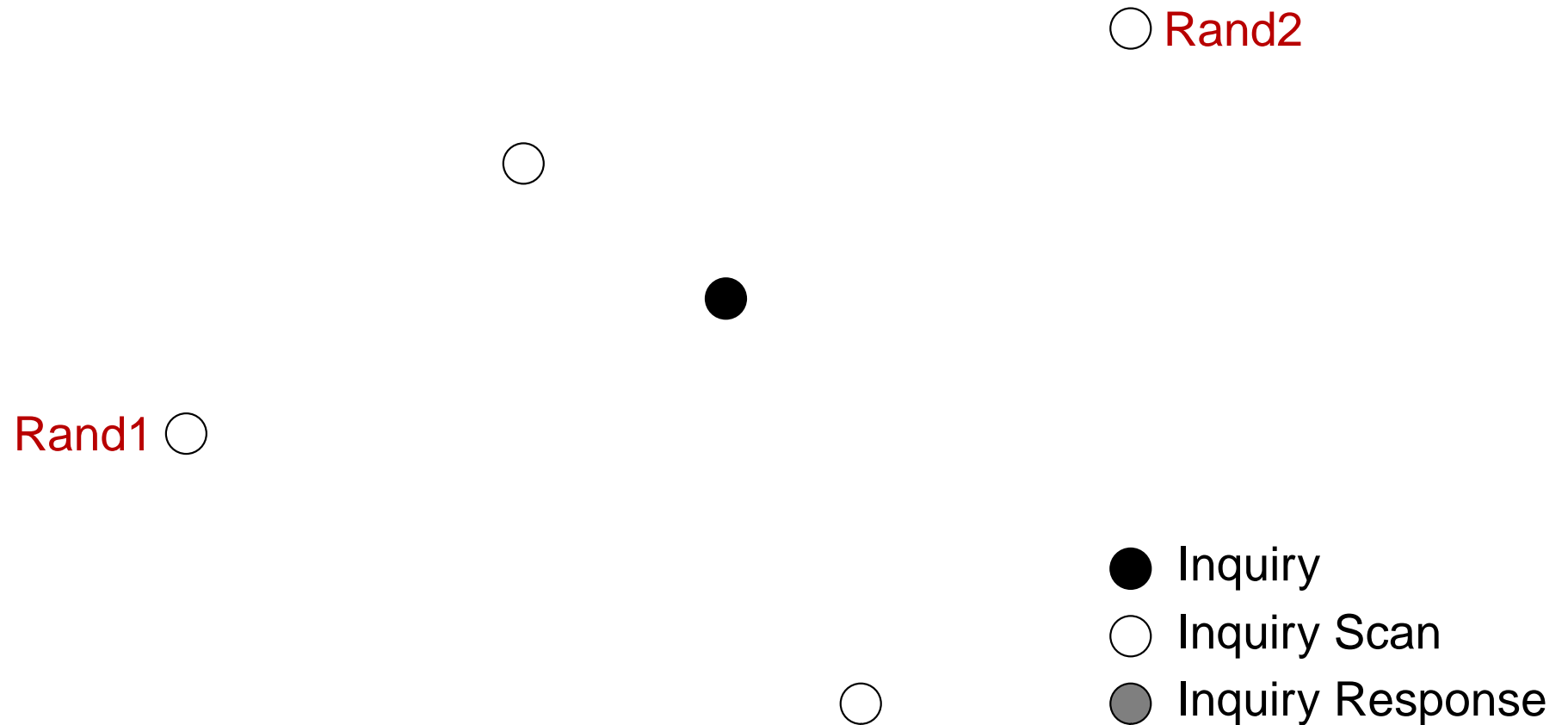
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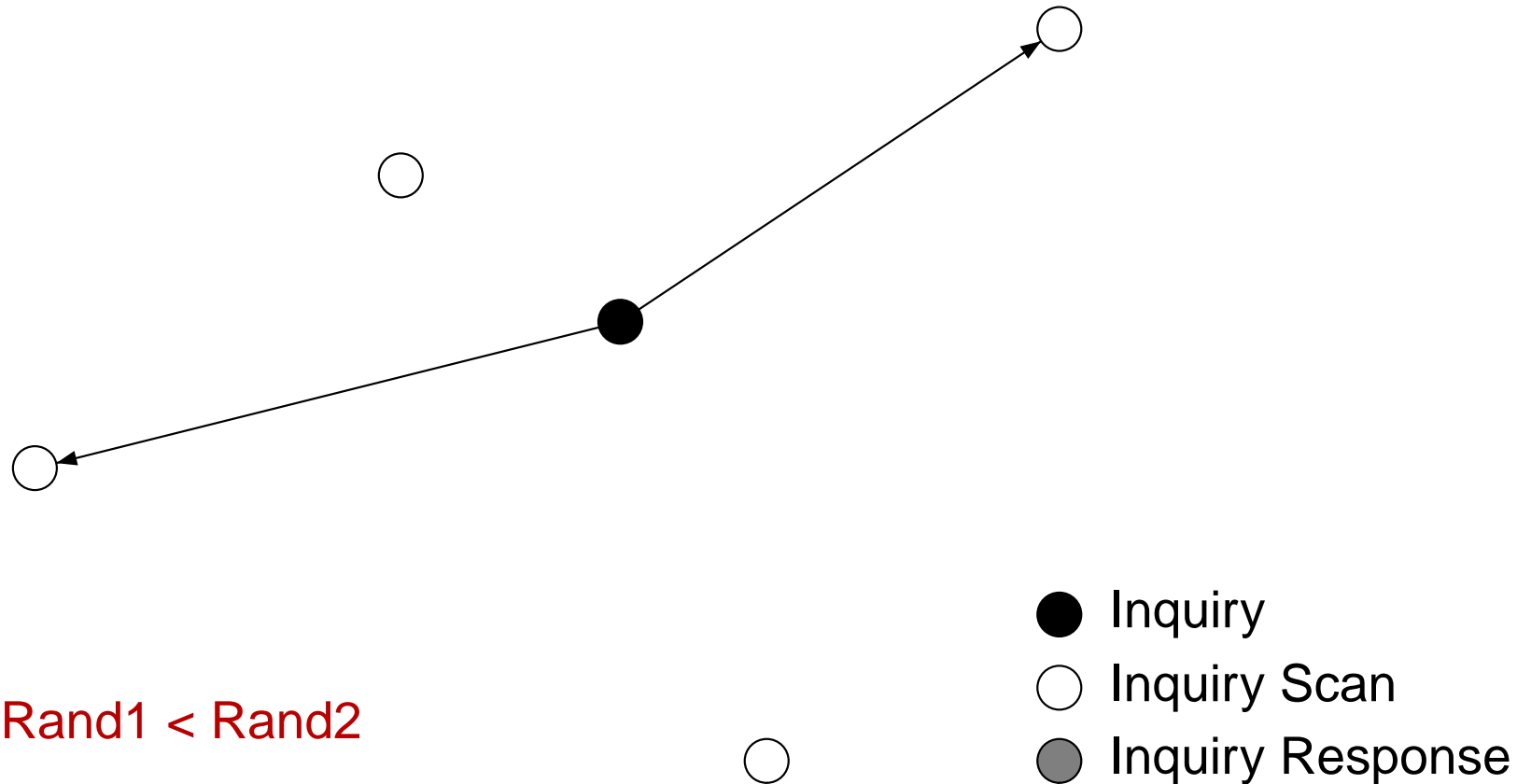
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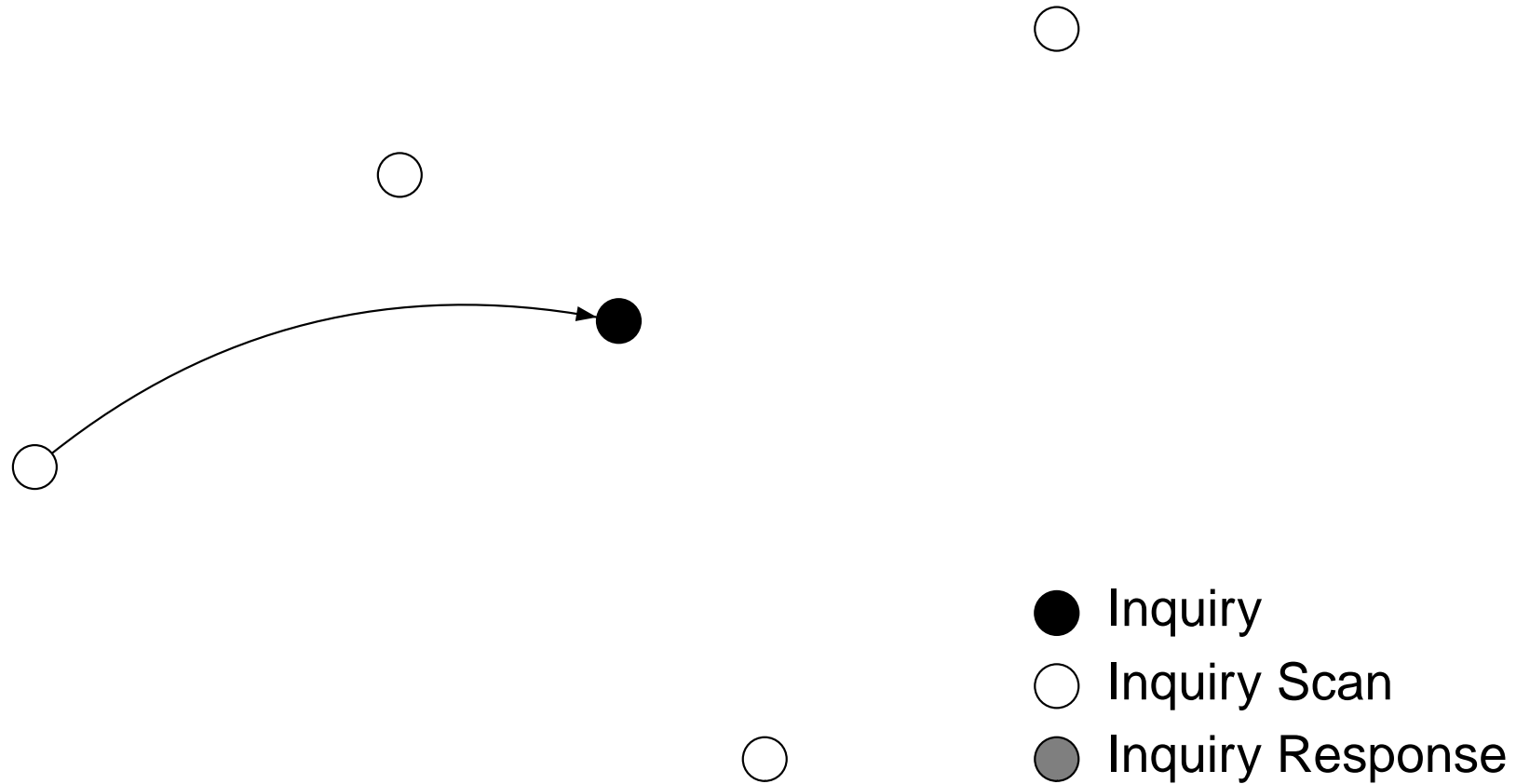
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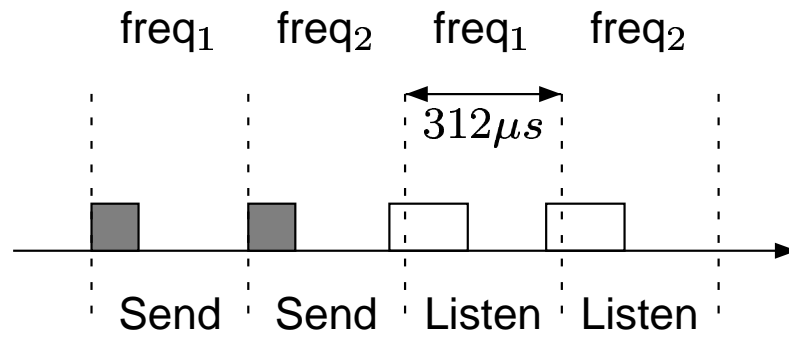
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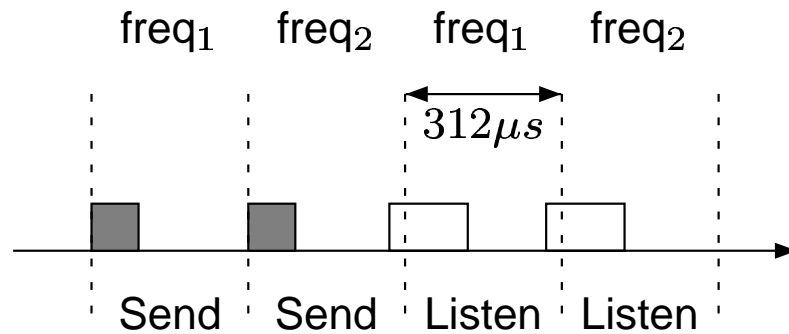
# The sender

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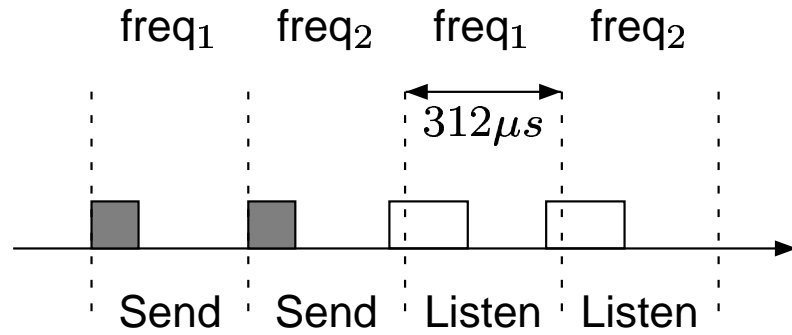


# The sender



$$\begin{aligned} freq &= [CLK_{16-12} + k \\ &+ (CLK_{4-2,0} - CLK_{16-12}) \bmod 16] \bmod 32 \end{aligned}$$

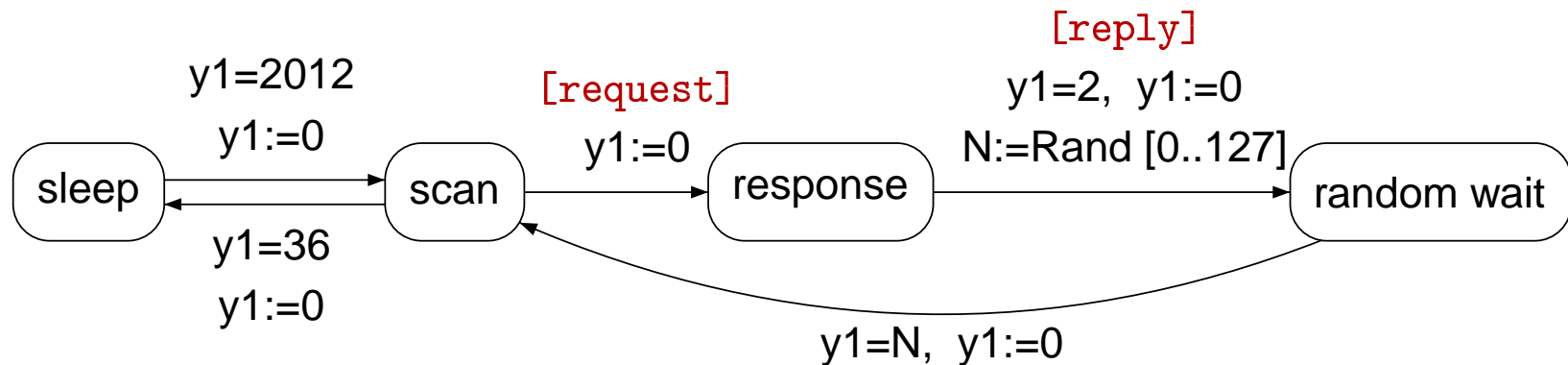
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1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
17	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1	2	19	20	21	22	23	24	25	26	27	28	29	30	31	32
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# The receiver



- $[request]$ : message sent by the sender
- $[reply]$ : message sent by the receiver
- need to compute the frequency at which the receiver is listening (phase)
- phase increased by one each time the receiver replies

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# Modelling the protocol

# Modelling formalism

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- randomised back-off
    - need probabilistic model
  - discrete time slots
  - no nondeterminism
    - no nondeterministic choice within a device
    - full synchronisation between devices
- discrete-time Markov Chains (DTMCs)

# Constants from Bluetooth standard

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- Sender changes state every time slot
- Receiver can wait for 2012 time slots without changing state
- 2 trains of 16 frequencies
- The trains change with time
- A train is repeated 256 times before switching
- The phase changes every 4096 slots
- A **Huge** model
- Too many possible initial states

# Receiver's frequencies

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```
module frequency1

    z1 : [1..phase]; // clock for phase
    f1 : [1..16]; // frequency of receiver
    o1 : [0..1]; // offset of receiver

    // update frequency (1 slot passes)
    [time] z1<phase -> (z1'=z1+1);
    [time] z1=phase -> (z1'=1) & (f1'=f1<16?f1+1:1)& (o1'=f1<16?o1:1-o1);
    // update frequency: something is sent by the receiver
    [reply] true -> (f1'=(f1<16)?f1+1:1) & (o1'=(f1<16)?o1:1-o1);

endmodule
```

# Abstractions (1): the sender

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[time] (x=0) -> (x'=1) ;  
[] (x=1) & (send=1) -> (send'=2) ;



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    ↓  
[time] (send=1) -> (send'=2) ;

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$$\begin{array}{l} [\text{time}] (x=0) \rightarrow (x'=1) ; \\ [] (x=1) \ \& \ (\text{send}=1) \rightarrow (\text{send}'=2) ; \\ \Downarrow \\ [\text{time}] (\text{send}=1) \rightarrow (\text{send}'=2) ; \end{array}$$

- no clock for the sender
- sender totally deterministic

# Abstractions (2): the receiver

- Initial execution:

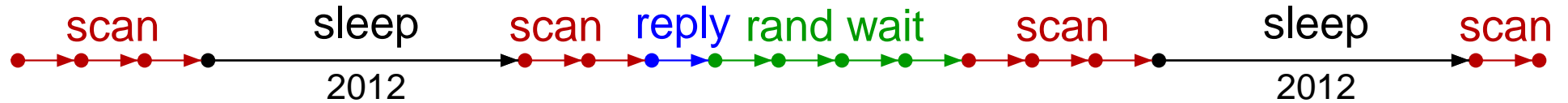


# Abstractions (2): the receiver

- Initial execution:



- Merge consecutive sleep transitions into one

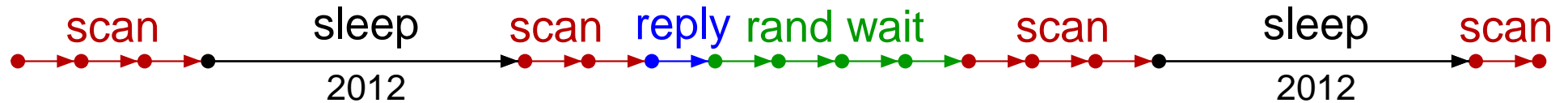


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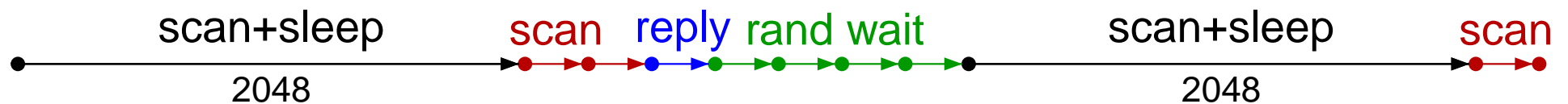
- Initial execution:



- Merge consecutive sleep transitions into one



- Formula success: decides if the receiver is going to hear something.
  - Merge scan with sleep when hears nothing



➔ works only for **one** receiver

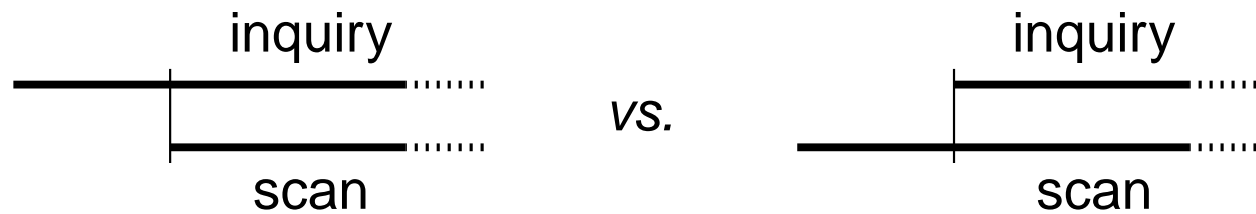
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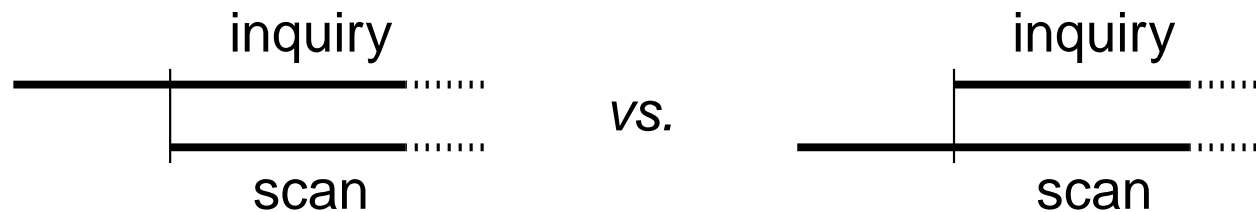
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- need to fix a scenario
- sender's state entirely determined by its clock
  - doesn't start inquiring in a precise state
- receiver's point of view
  - a sender is already inquiring
  - we start when the receiver scans

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**But** ... still 17 thousand million initial states



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# Verification and Results

# Verification with PRISM

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Model checking vs. simulation

- examine lower-level detail
- worst case, not only average

New version of PRISM including:

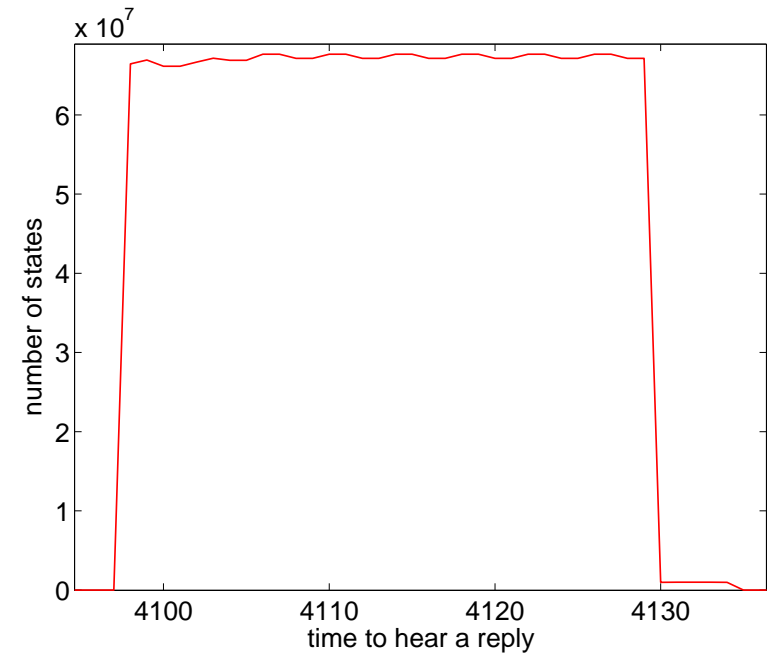
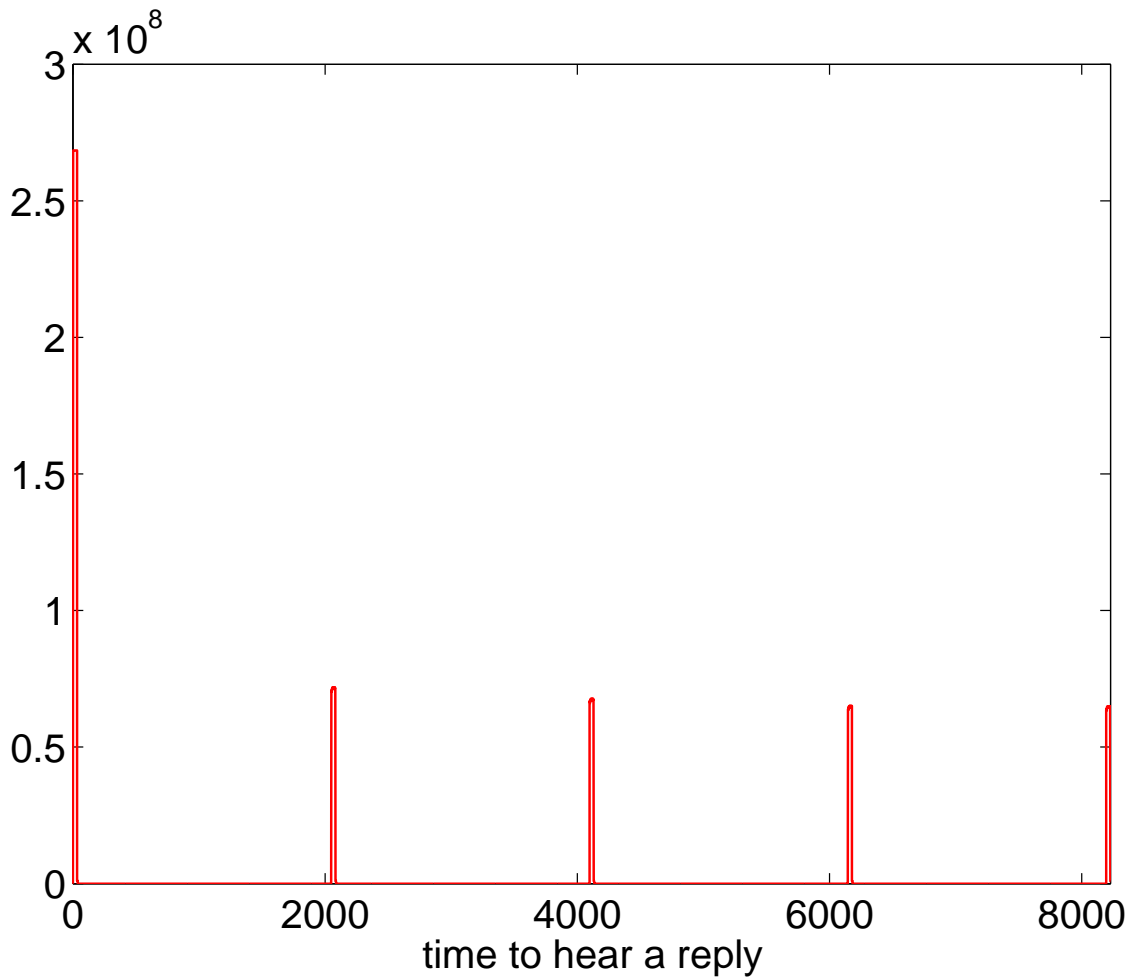
- computation of expected time  
[label,cost] condition -> update  
R=? [F rec=2]
- multiple initial states  
Predicate over variables vs. a value for each variable
- additional queries for results over many states  
R=? [F rec=2 {"init"}{min}{max}]

# Expected time to receive one reply

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- Very big models → symbolic implementation (MTBDDs)
- Initial states split into 32 classes (possible initial frequencies)
- 32 models of around 3 thousand million states each
- 55-57 seconds to build one model
- 3-4 seconds to check the property

# Graph of the results



# Analysis of the results

- Time to reply to one message: min 2, max 8,229 slots (2.5 seconds)
- probability of replying to message after sleeping  $N$  times

$N$	0	1	2	3	4
$p$	0.5003	0.6335	0.7591	0.8797	1

- Analysis of the worst case expected time

1 2 3 20 21 22 23 24 25 26 27 28 29 30 31 32

17 18 19 20 5 6 7 8 9 10 11 12 13 14 15 16

17 18 19 20 21 6 7 8 9 10 11 12 13 14 15 16

1 2 3 4 5 6 23 24 25 26 27 28 29 30 31 32

- sender starts on frequency 3
- receiver starts on frequency 2
- last repetition of the train

# Expected time to receive two replies

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- Size of the models: 51 thousand million states
- Time to build the models: 30 minutes
- Time to check the property: 80 minutes
- Maximum expected time: 16,502 slots (5 seconds)

# It's not over yet!!!

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- Count up to more replies
- Consider more than one receiver
- Compare version 1.1 and 1.2

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**Problem:**

State space!!!



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## Problem:

State space!!!

## Solutions:

- Simulation?
- Scaling?
- Abstraction?